## 13.1-Solutions

Homogeneous mixtures can be classified according to the size of their particles as either solution or colloids
Solution is the common class of homogenous mixture. They are transparent, may be colored and can't be physically separated.
Colloids are often murky or opaque to light. (E.g: milk or fog)
Suspensions have larger particles than colloids. Their particles separate out on standing and are visible


Table 13.1 Some Different Kinds of Solutions

| Gas in gas | Air $\left(\mathrm{O}_{2}, \mathrm{~N}_{2}, \mathrm{Ar}\right.$, and other gases $)$ |
| :--- | :--- |
| Gas in liquid | Carbonated water $\left(\mathrm{CO}_{2}\right.$ in water) |
| Gas in solid | $\mathrm{H}_{2}$ in palladium metal |
| Liquid in liquid | Gasoline (mixture of hydrocarbons) |
| Liquid in solid | Dental amalgam (mercury in silver) |
| Solid in liquid | Seawater $(\mathrm{NaCl}$ and other salts in water) |
| Solid in solid | Metal alloys, such as sterling silver $(92.5 \% \mathrm{Ag}, 7.5 \% \mathrm{Cu})$ |

### 13.2 Enthalpy Changes and the Solution Process

## A good rule of thumb, "like dissolves like"

Solution will form when the three types of intermolecular interactions are similar in kind and magnitude
Common intermolecular forces that can be use to predict the formation of a solution:

- Ion-ion interaction $\left(\mathrm{Na}^{+} \mathrm{Cl}^{-}\right)$
- Ion-dipoles $\left(\mathrm{Na}^{+} \mathrm{H}_{2} \mathrm{O}, \mathrm{Cl}^{-} \mathrm{H}_{2} \mathrm{O}\right)$
- Hydrogen bonding (OH, NH, HF) (polar interaction)
- Dipole-dipole (polar interaction)
- London dispersion (nonpolar molecules)


$\Delta H_{\text {soln }}$ is negative if solvent-solute interactions are dominant.

The solute-solvent interactions are greater than the sum of the solute-solute and solvent-solvent interactions.

Simply put, three processes affect the energetics of the process:
_ Separation of solute particles
$\Delta \mathrm{H}_{1}$ ( this is always endothermic)
_ Separation of solvent particles $\Delta \mathrm{H}_{2}$ ( this too is always endothermic)
_ New interactions between solute and solvent $\Delta \mathrm{H}_{3}$ ( this is always exothermic)

The overall enthalpy change associated with these three processes:
$\Delta \mathbf{H}_{\text {soln }}=\Delta \mathrm{H}_{1}+\Delta \mathrm{H}_{2}+\Delta \mathrm{H}_{3} \quad$ (Hess's Law)


$$
\Delta \boldsymbol{H}_{\text {soln }}>0
$$

$\Delta H_{\text {soln }}$ is positive if solvent-solute interactions are not dominant.

The solute-solvent interactions are less than the sum of the solute-solute and solvent-solvent interactions.


Additional water molecules
The sodium and chloride ions are hydrated.
then surround the ion and
stabilize it by means of ion-

## 13.3 - Predicting Solubilities

Like all chemical and physical processes, the dissolution of a solute in a solvent has associated with it a Gibbs freeenergy change, $\Delta \mathrm{G}=\mathrm{H}$ - TS, whose value describes its spontaneity. If $\Delta \mathrm{G}$ is negative, the process is spontaneous and the substance dissolves; if $\Delta \mathrm{G}$ is positive, the process is nonspontaneous and the substance does not dissolve.
If we defined the enthalpy of solution $\Delta \mathrm{H}_{\text {soln }}$ as the heat released or absorbed upon solution formation, and similarly the entropy of solution, $\Delta \mathrm{S}_{\text {sol }}$ is the entropy change that occurs when the solute dissolves in the solvent.

When one liquid dissolves in another, randomness increases as the different molecules intermingle


Table 13.2 Some Enthalpies and Entropies of Solution in Water at

| Substance | $\boldsymbol{\Delta} \boldsymbol{H}^{\circ}{ }_{\text {soln }}(\mathbf{k J} / \mathrm{mol})$ | $\boldsymbol{\Delta} \boldsymbol{S}_{\text {soln }}[\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})]$ |
| :--- | :---: | :---: |
| LiCl | -37.0 | 10.5 |
| NaCl | 3.9 | 43.4 |
| KCl | 17.2 | 75.0 |
| LiBr | -48.8 | 21.5 |
| NaBr | -0.6 | 54.6 |
| KBr | 19.9 | 89.0 |
| KOH | -57.6 | 12.9 |

Beside using intermolecular forces and polarity to predict the solubility, how can we predict if a solute will be soluble in a given solvent? Thermodynamics tells us that if the free-energy change of solution formation is negative, then the process will be spontaneous.
Example: Predict the solubilities of NaCl in water ate $25^{\circ} \mathrm{C}$.

### 13.4 Concentration Units for Solutions

In daily life, it's often sufficient to describe a solution as either dilute or concentrated. In scientific work, though, it's usually necessary to know the exact concentration of a solution-that is, to know the exact amount of solute dissolved in a certain amount of solvent. There are many ways of expressing concentration:

$$
\begin{gathered}
\text { Molarity }(\mathbf{M})=\frac{\text { Moles of solute }}{\text { Liters of solution }} \\
\text { Mole fraction }(\mathbf{X})=\frac{\text { Moles of component }}{\text { Total moles making up solution }} \\
\text { Mass percent }=\frac{\text { Mass of component }}{\text { Total mass of solution }} \times 100 \% \\
\text { Molality }(\boldsymbol{m})=\frac{\text { Moles of solute }}{\text { Mass of solvent }(\mathrm{kg})}
\end{gathered}
$$

A summary of the four most common units for expressing concentration, together with a comparison of their relative advantages and disadvantages

| Name | Units | Advantages | Disadvantages |
| :--- | :--- | :--- | :--- |
| Molarity (M) | $\frac{\text { mol solute }}{\text { L solution }}$ | Useful in stoichiometry; by volume | Temperature-dependent; must know density to find <br> solvent mass |
| Mole fraction (X) | none | Temperature-independent; useful in special <br> applications | Measure by mass; must know density to convert to <br> molarity |
| Mass \% | $\%$ | Temperature-independent; useful for small amounts | Measure by mass; must know density to convert to <br> molarity |
| Molality $(m)$ | $\frac{\text { mol solute }}{\text { kg solvent }}$ | Temperature-independent; useful in special <br> applications | Measure by mass; must know density to convert to <br> molarity |

Example: What is the molality of a solution made by dissolving 1.45 g of table sugar (sucrose, $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$ ) in 30.0 mL of water? The molar mass of sucrose is $342.3 \mathrm{~g} / \mathrm{mol}$, and the density of water is $1.00 \mathrm{~g} / \mathrm{mL}$.

Example: Nitrate, $\mathrm{NO}_{3}$ enters the water supply from fertilizer runoff or leaking septic tanks. The legal limit in drinking water is 10.0 ppm because infants who drink water exceeding this level can become seriously ill. What mass of nitrate $(\mathrm{mg})$ is present in 1.5 L of water with a concentration of 10.0 ppm ? (Assume the density of water is 1.0 $\mathrm{g} / \mathrm{mL}$.)

## 13.5- Factors that affects solubility

When there is an attraction between the particles of the solute and solvent.
When a polar solvent such as water dissolves polar solutes such as sugar, and ionic solutes such as NaCl .
When a nonpolar solvent such as hexane $\left(\mathrm{C}_{6} \mathrm{H}_{14}\right)$ dissolves nonpolar solutes such as oil or grease.

- Saturated solution: A solution containing the maximum possible amount of dissolved solute at equilibrium.


## dissolve

Solute + Solvent $\underset{\text { crystallize }}{ }$ Solution

- Supersaturated Solution: A solution containing a greater-than-equilibrium amount of solute.

- Unsaturated solution: a solution containing less than the equilibrium amount of solute

When there is an attraction between the particles of the solute and solvent.
When a polar solvent such as water dissolves polar solutes such as sugar, and ionic solutes such as NaCl .
When a nonpolar solvent such as hexane $\left(\mathrm{C}_{6} \mathrm{H}_{14}\right)$ dissolves nonpolar solutes such as oil or grease.

## Effect of Temperature on Solubility

Solubility curves can be used to predict whether a solution with a particular amount of solute dissolved in water is saturated (on the line), unsaturated (below the line), or supersaturated (above the line)

## Solubility

- depends on temperature
- most solids increases as temperature increases.
- Hot tea dissolves more sugar than does cold tea because the solubility of sugar is much greater in higher temperature
- There is no obvious correlation between structure and solubility or between solubility and temperature.
- When a saturated solution is carefully cooled, it becomes a supersaturated solution because it contains more solute than the solubility allows.


Example: The solubility of KCl at $50^{\circ} \mathrm{C}$ is $42 \mathrm{~g} / 100 \mathrm{~g}$. If 20.0 g of KCl was dissolved in 35.0 g water, would the solution be unsaturated, saturated or supersaturated?

## Effects of Pressure on Solubilities - Gases in Solution

- In general, the solubility of gases in water increases with increasing mass as the attraction between the gas and the solvent molecule is mainly dispersion forces.
- Larger molecules have stronger dispersion forces.

Henry's law states

- the solubility of a gas in a liquid is directly related to the pressure of that gas above the liquid.
- at higher pressures, more gas molecules dissolve in the liquid.


## Solubility $=k \cdot \boldsymbol{P}$

- where
- $k$ is the Henry's law constant for that gas in that solvent at that temperature
- $P$ is the partial pressure of the gas above the liquid.


Henry's Law is what (in a manner of thinking) gives soda pop its fizz. The bubbling that occurs when a can of soda is opened results from the reduced pressure of carbon dioxide over the liquid. At lower pressure, the carbon dioxide is less soluble and bubbles of solution.

Example: Calculate the concentration of $\mathrm{CO}_{2}$ in a soft drink that is bottled with a partial pressure of $\mathrm{CO}_{2}$ of 4.0 atm over the liquid at $25^{\circ} \mathrm{C}$. The Henry's law constant for $\mathrm{CO}_{2}$ in water at this temperature is $3.1 \times 10^{-2} \mathrm{M} / \mathrm{atm}$.

## 13.6 - Physical Behavior of Solutions: Colligative Properties

Colligative Properties: Properties that depend on the amount of a dissolved solute but not on its chemical identity.

- Vapor-Pressure Lowering

Boiling-Point Elevation

- Freezing-Point Depression

Osmotic Pressure
Solutions of ionic substances often have a vapor pressure significantly lower than predicted, because the ion-dipole forces between the dissolved ions and polar water molecules are so strong.

### 13.7 Vapor-Pressure Lowering of Solutions: Raoult's Law



Beakers with equal liquid levels of pure solvent and a solution are place in a bell jar. Solvent molecules evaporate from each one and fill the bell jar, establishing an equilibrium with the liquids in the beakers.

When equilibrium is established, the liquid level in the solution beaker is higher than the solution level in the pure solvent beaker - the thirsty solution grabs and holds solvent vapor more effectively

The vapor pressure of a volatile solvent above a solution is equal to its mole fraction of its normal vapor pressure, $P^{\circ}$

- since the mole fraction is always less than 1, the vapor pressure of the solvent in solution will always be less than the vapor pressure of the pure solvent

$$
P_{\text {total }}=P_{A}+P_{B}=\left(P_{A}^{\circ} X_{A}\right)+\left(P_{B}^{\circ} X_{B}\right)
$$



Example: The vapor pressure of pure water at $25^{\circ} \mathrm{C}$ is 23.8 atm . Determine the vapor pressure (torr) of water at $25^{\circ} \mathrm{C}$ above a solution prepared by dissolving 18.0 g glucose ( $\mathrm{MW}=180.0 \mathrm{~g} / \mathrm{mol}$ ) in 95.0 g of water?

## Solutions with a Nonvolatile Solute

- according to Raoult's Law, the effect of solute on the vapor pressure simply depends on the number of solute particles
- when ionic compounds dissolve in water, they dissociate - so the number of solute particles is a multiple of the number of moles of formula units
- the effect of ionic compounds on the vapor pressure of water is magnified by the dissociation
- since NaCl dissociates into 2 ions, $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$, one mole of NaCl lowers the vapor pressure of water twice as much as 1 mole of $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$ molecules would
- When $\mathrm{NaCl}(s)$ dissolves in water, the reaction can be written as
- $\mathrm{NaCl}(s) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{Na}^{+}(a q)+\mathrm{Cl}^{-}(a q)$
- solid separation of ions
- If an ionic salt is soluble in water, it is because the ion dipole
- Interactions are strong enough to overcome the lattice energy of the salt crystal.


A further complication is that ionic substances rarely dissociate completely, so a solution of an ionic compound usually contains fewer particles than the formula of the compound would suggest. The actual extent of dissociation can be expressed as a van't Hoff factor (i).

$$
\text { Van't Hoff Factor : } i=\frac{\text { Moles of particles in solution }}{\text { Moles of solute dissolved }}
$$

- For sodium chloride, the predicted value of $\boldsymbol{i}$ is 2 . For a 0.5 m solution of sodium chloride, the experimental value for $i$ is $\mathbf{1 . 9}$.

|  | Van't Hoff Factors at <br> O.OS m Concentration <br> in Aqueous Solution |  |
| :--- | :--- | :---: |
| Solute | $i$ Expected | i Measured |
| Nonelectrolye | 1 |  |
| NaCl | 2 | 1 |
| $\mathrm{MgSO}_{4}$ | 2 | 1.9 |
| $\mathrm{MgCl}_{2}$ | 3 | 1.3 |
| $\mathrm{~K}_{2} \mathrm{SO}_{4}$ | 3 | 2.7 |
| $\mathrm{FeCl}_{3}$ | 4 | 2.6 |

- The smaller than expected value for $i$ is due to incomplete dissociation of ionic compounds. As the concentration decreases, the experimental value for $i$ increases until it reaches the theoretical maximum (decreased occurrence of ion-pairs in solution also plays a factor).

Example: What is the vapor pressure in mmHg of a solution made by dissolving 18.30 g of NaCl in 500.0 g of $\mathrm{H}_{2} \mathrm{O}$ at $70^{\circ} \mathrm{C}$, assuming a van't Hoff factor of 1.9? The vapor pressure of water at $70^{\circ} \mathrm{C}$ is 233.7 mmHg .

### 13.8 Boiling-Point Elevation and Freezing-Point Depression

We saw in Section 11.3 that the vapor pressure of a liquid rises with increasing temperature and that the liquid boils when its vapor pressure equals atmospheric pressure. Because a solution of a nonvolatile solute has a lower vapor pressure than a pure solvent has at a given temperature, the solution must be heated to a higher temperature to cause it to boil. Figure 13.14 shows how the phase diagram for a solution is different than that of a pure solvent.
 temperature. As a result, the freezing point of the solution is lower than that of the pure solvent by an amount $\Delta T_{f}$.

The change in boiling point $\mathrm{T}_{\mathrm{b}}$ for a solution is proportional to the number of solute particles present and can be related to the molality of the solution

## Dang 10

$$
\left(\mathbf{B} \mathbf{P}_{\text {solution }}-\mathbf{B} \mathbf{P}_{\text {solvent }}\right)=\Delta \mathrm{T}_{\mathrm{b}}=\mathrm{m} \cdot \mathrm{~K}_{\mathrm{b}}
$$

The freezing-point depression for a solution relative to that of a pure solvent depends on the concentration of solute particles, just as boiling-point elevation does.

| $\begin{gathered} \left(F P_{\text {solvent }}-F P_{\text {solution }}\right)=\Delta \mathrm{T}_{\mathrm{f}}=\mathrm{m} \cdot K_{\mathrm{f}} \\ \Delta \mathrm{~T}_{\mathrm{f}}=\mathrm{K}_{\mathrm{f}} \cdot \mathrm{~m} \end{gathered}$ |  |
| :---: | :---: |
| For ionic substances: | $\begin{aligned} \Delta \mathrm{T}_{\mathrm{b}} & =\mathrm{K}_{\mathrm{b}} \bullet \mathrm{m} \cdot \mathrm{i} \\ \Delta \mathrm{T}_{\mathrm{f}} & =\mathrm{K}_{\mathrm{f}} \bullet \mathrm{m} \cdot \mathrm{i}\end{aligned}$ |

Table 13.4 Molal Boiling-Point-Elevation Constants $\left(K_{b}\right)$, and Molal Freezing Point-Depression Constants ( $K_{f}$ )

| Substance | $K_{\mathrm{b}}\left[\left({ }^{\circ} \mathrm{C} \cdot \mathbf{k g}\right) / \mathrm{mol}\right]$ | $K_{\mathrm{f}}\left[\left({ }^{\circ} \mathrm{C} \cdot \mathbf{k g}\right) / \mathrm{mol}\right]$ |
| :--- | :---: | :---: |
| Benzene $\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)$ | 2.64 | 5.07 |
| Camphor $\left(\mathrm{C}_{10} \mathrm{H}_{16} \mathrm{O}\right)$ | 5.95 | 37.8 |
| Chloroform $\left(\mathrm{CHCl}_{3}\right)$ | 3.63 | 4.70 |
| Diethyl ether $\left(\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}\right)$ | 2.02 | 1.79 |
| Ethyl alcohol $\left(\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}\right)$ | 1.22 | 1.99 |
| Water $\left(\mathrm{H}_{2} \mathrm{O}\right)$ | 0.51 | 1.86 |

Example: What is the normal boiling point in ${ }^{\circ} \mathrm{C}$ of an antifreeze solution prepared by dissolving 616.9 g of ethylene glycol $\left(\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}_{2}\right)$ in 500.0 g of water? The molal boiling point elevation constant for water is 0.51 ${ }^{\circ} \mathrm{C} \cdot \mathrm{kg} / \mathrm{mol}$ and molar mass of ethylene glycol is $62.07 \mathrm{~g} / \mathrm{mol}$

Example: How many g of ethylene glycol, $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}_{2}$, must be added to $1.0 \mathrm{~kg} \mathrm{H} \mathrm{H}_{2} \mathrm{O}$ to give a solution that boils at $105^{\circ} \mathrm{C}$ ? $\mathrm{K}_{\mathrm{b}}=0.512\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.

Example: What is the freezing point in ${ }^{\circ} \mathrm{C}$ of a solution prepared by dissolving 7.40 g of $\mathrm{MgCl}_{2}$ in 110 g of water. Assume $\mathrm{MgCl}_{2}$ has completely ionized.

### 13.9 Osmosis and Osmotic Pressure

Certain materials, including those that make up the membranes around living cells, are semipermeable. That is, they allow water or other smaller molecules to pass through, but they block the passage of larger solute molecules or solvated ions.

Osmosis: The passage of solvent through a semipermeable membrane from the less concentrated side to the more concentrated side.

- Solvent flows from a high solvent concentration to a low solvent concentration. Or, solvent flows from a low solute concentration to a high solute concentration.
- the level of the solution with the higher solute concentration rises.
- the concentrations of the two solutions become equal with time.

Osmotic Pressure ( $\mathbf{P}$ ): The amount of pressure necessary to cause osmosis to stop.

- Osmotic pressure can be calculated using molarity since it is calculated at a specific temperature and thus no need for temperature-independent
units.

$$
\Pi=\text { MRT }
$$

$\mathrm{R}=0.08206 \mathrm{~L} \cdot \mathrm{~atm} / \mathrm{K} \cdot \mathrm{mol}$


Suppose a semipermeable membrane separates a $4 \%$ starch solution from a $10 \%$ starch solution. Starch is a colloid and cannot pass through the membrane, but water can. What happens?


Example: The osmotic pressure of a solution containing 5.87 mg of an unknown protein per 10.0 mL of solution is 2.45 torr at $25^{\circ} \mathrm{C}$. Find the molar mass of the unknown protein.

Example: Figure below shows the transport of solvent across the membrane of red blood cells in solutions of varying concentration.
(a) What is the osmotic pressure of a solution inside a red blood cell with a total concentration of dissolved particles of 0.30 M ?


In a hypertonic solution, the
In a hypertonic solution, the
solute concentration in the solution is greater than that inside the cell. There is a net
transfer of water from the cell transfer of water from the cell
to the solution causing the cell to the solution causing
to shrivel and shrink.


In a isotonic solution, the solution is the same as that inside the cell. There is no net transfer of water across the cell membrane.


In a hypotonic solution, the
solute concentration in the solution is less than that inside the cell. There is a net transfer of water across the cell
membrane into the cell
causing the cell to swell and becomes too high.
(b) Red blood cells rupture if the pressure differential across their membrane is 5 atm or higher. Would the blood cells rupture if they were placed in pure water?

